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مسألة فكيته - زيغو للدوال شديدة القرب من التحذب ذات الرتبة بيتا
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- Abstract** : Let A be the class of functions $f(z) = z + a_2z^2 + a_3z^3 + \dots$ which are analytic in the unit disc $D = \{z: |z| < 1\}$. Let S be the subclass of A of, univalent functions. A classical result of Fekete and Szego determines the maximum value of $|a_3 - \lambda a_2^2|$ as a function of the real parameters, for $f \in S$. This problem has attracted considerable attention when f ranges over certain subclasses of A . The problem has equal importance, if not more, when $f \in S_p(b)$. The Fekete -Szego problem has served as a main source for research problems in geometric function theory. It is the foundation stone over which a subject and a whole bulk of results rest. This dissertation is subdivided into three chapters, In the first chapter we give some basic definitions, notations and preliminary concepts. The second chapter introduces the classes $S_p(b)$ and $C_p(b)$ of strongly starlike and convex functions of order α and complex type β respectively. Sharp bounds are obtained for $\max |a_3 - \lambda a_2^2|$ when $f \in S_p(b)$. In Chapter three, we study the Fekete -Szego problem for the subclass K_α of normalized functions which are analytic and strongly close - to - convex of order α . This seems to be the most interesting result of the present work. This problem is still far from its complete solution. (cf. MR # 92e: 3004 and MR # 93e: 30029).
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